The calculation of optical spectra

Tout de même, avant de mourir, je voudrais deviner ce que c'est, la couleur.

Pablo Picasso

Colours
State of the art
Why is it difficult?
Do you need to be a superhero?

Gravitational waves





Merging of two giant black holes
1400000000 light years
1.5 billion €

Standard model of elementary particles



238 particles
More than one million experiments
13 billion €



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Colour of life (porphyrins)



Colour of pigments (minerals)



Colour of gemstones (minerals)





• Visible range: 400 nm to 700 nm or 1.8 eV to 3.0 eV





• The eye distinguises 150 hues: < 10 meV



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The colour of grass



- Time-dependent density functional theory study of the electronic excitation spectra of Chlorophyllide a and Pheophorbide a in solvents, Z-W Qu, H. Zhu, V May, R Schinke, J. Phys. Chem. B. (2009) 113 4817
- The predicted excitation energies and oscillator strengths now agree much better with experiments







Figure 3. TDDFT predicted electronic absorption spectra in gas phase (in red dashed sticks) and in ethanol for pheophorbide a and in methanol for chlorophyllide a (in black solid sticks) within PCM model. The corresponding experimental spectra in solvents from refs 2 and 3 (in black solid lines) are also included for comparison.

Porphyrins



- Challenging density functional theory calculations with hemes and porphyrins,
 S. P. de Visser, M. J. Stillman, Int. J. Mol. Sci. (2016) 17 519
- Abstract: In recent years computational tools have improved considerably and now can reproduce experimental spectroscopic studies
- The Q-band is predicted to be at 535 nm, but is observed at 578 nm (0.17 eV)



Colour of fayalite Fe₂SiO₄





O.V. Krasovska et al., Am. Min. 82 (1997) 672

What colour can we compute?

- Perspective: Fundamental aspects of time-dependent density functional theory, N. T. Maitra, J. Chem. Phys. (2016) **144**, 220901
- Fully parameter-free calculation of optical spectra for insulators,
 semiconductors and metals from a simple polarization functional, J. A. Berger,
 Phys. Rev. Lett. (2015), 115, 137402
- Time-dependent density functional theory calculations for the excitation spectra of III-V ternary alloys, Zhenhua Ning, Ching-Tarng Liang, Yia-Chung Chang, Phys. Rev. B (2017), 96, 085202
- Solution of the Bethe-Salpeter equation without empty electronic states: Application to the absorption spectra of bulk systems, D. Rocca, Yuan Ping, R. Gebauer, G. Galli, Phys. Rev. B (2012), 85, 045116
 - Zn-VI quasiparticle gaps and optical spectra from many-body calculations, A.
 Riefer, N. Weber, J. Mund, D.R. Yakovlev, M. Bayer, A. Schindlmayr, C.
 Meier W.G. Schmidt, J. Phys.: Cond. Matt. (2017), 85, 045116

Semiconductors

Zn-VI quasiparticle gaps and optical spectra from many-body calculations, A. Riefer, N. Weber, J. Mund, D.R. Yakovlev, M. Bayer, A. Schindlmayr, C. Meier W.G. Schmidt, J. Phys.: Cond. Matt. (2017), **85**, 045116







Metals

 Fully parameter-free calculation of optical spectra for insulators, semiconductors and metals from a simple polarization functional, J. A. Berger, Phys. Rev. Lett. (2015), 115, 137402

excitons



Drude tails

FIG. 3 (color online). The optical absorption spectra of diamond and copper. Solid line (black), polarization functional (PF); dashed line (red), RPA; dotted line (blue), experiment from Ref. [47] (diamond) and Refs. [48] and [49] (Cu).

Transition metal oxides $[M(H_2O)_6]^{n+}$

- Multireference ab initio study of ligand field d-d transitions in octahedral transition-metal oxide clusters, Yang Yang, M.A. Ratner, G.C. Schatz, J. Phys. Chem. (2014), 118, 29196
 - Multiconfigurational multireference methods (CASSCF, CASPT2, MRCI)



- Good bond length
- Good ligand-to-metal charge transfer energy

Transition metal oxides $[M(H_2O)_6]^{n+}$

 Multireference ab initio study of ligand field d-d transitions in octahedral transition-metal oxide clusters, Yang Yang, M.A. Ratner, G.C. Schatz, J. Phys. Chem. (2014), 118, 29196

Table 3. Multireference d–d Transition Energies for $Fe(H_2O)_6^{3+}$ (eV)										
	state	CASPT2(5,5)	CASPT2(5,10)	MRCI(5,5)	exp					
	⁶ A _g	0.00	0.00	0.00	0.00					
	${}^{4}B_{1g}$	2.89	2.85	3.02	1.56					
	${}^{4}B_{1g}$	n/a	n/a	3.74	2.29					
	⁴ A _g	3.78	3.80	4.08	3.01					
	⁴ A _g	3.82	3.84	4.13	3.05					
	${}^{4}A_{g}$	3.82	3.84	4.13						

Table 13. Calculated	d-d Transition	Energies for d ³
$[Cr(H_2O)_6]^{3+}$ (eV)		C

state	CASSCF(3,5)	$CASPT2(3,5)^a$	MRCI(3,5)	exp
⁴ A _g	0.00	0.00	0.00	0.00
${}^{4}B_{1g}/B_{2g}/B_{3g}$	1.69	1.77	1.79	2.16
${}^{4}B_{1g}/B_{2g}/B_{3g}$	2.70	2.68	2.77	3.05
${}^{4}B_{1g}/B_{2g}/B_{3g}$	4.36	4.28	4.42	4.69
² A _g	2.41	2.23	2.35	2.60
$^{2}A_{g}$	2.41	2.23	2.35	2.60
${}^{2}A_{\sigma}$	3.71			

Ruby : Cr^{3+} in Al_2O_3





Optical spectra of ruby

First-principles calculation of ground and excited-state absorption spectra of ruby and alexandrite considering lattice relaxation, S. Watanabe, T. Sasaki, R. Taniguchi, T. Ishii, K. Ogasawara, Phys. Rev. B (2009), **79**, 075109





Further calculations

- Comparative study of absorption spectra of V^{2+} , Cr^{3+} , and Mn^{4+} in α - Al_2O_3 based on first-principles configuration-interaction calculations, M. Novita and K. Ogasawara, J. Phys. Soc. Japan (2012) **81** 104709 + 4 other papers until 2016
- Intra- and inter-atomic optical transitions of Fe, Co, and Ni ferrocyanides studied using firstprinciples many-electron calculations, S. Watanabe, Y. Sawada, M. Nakaya, M. Yoshino, T. Nagasaki, T. Kamemaya, T. Torimoto, Y. Inaba, H. Takahashi, K. Takeshita, J. Once, J. Appl. Phys. (2016) 119 235102

Expt.

5

Calc.





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Ruby and emerald





Chromium in alumina

Chromium in beryl

Aquamarine and heliodore



Iron in beryl





Transition metals

• Transitions in the range 1.8 eV to 3 eV:

3d orbitals are localized

3d orbitals are extended

3d orbitals are almost degenerate



Fig. 1. A schematic view of the splitting of the five-fold 3*d* orbitals under cubic crystal field. The transition metal is located at the center of the oxygen octahedra (shown in blue).

Calculation of transition energies

Transitions in the range 1.8 eV to 3 eV:

- Accuracy in the 10 meV range
- No low-energy effective Hamiltonian like in magnetism
- 3d orbitals are localized
 - Strong interaction (many-body techniques)
 - Strong excitonic (electron-hole) interaction (Bethe-Salpeter)
 - 3d orbitals are extended
 - Influence of the crystal host
 - Coupling between transition metals (sapphire)

Calculation of transition energies

3d orbitals are almost degenerate

- Green function techniques are not applicable
- High sensitivity to external perturbation
- Transitions metal impurities
 - Position of the TM atom in the structure (heliodore and aquamarine)
 - Deformation of the crystal structure
 - Possible clustering

Calculation of transition intensities

Which transition operator?
Selection rules
Role of vibrations

Electric dipole transitions

 Calculated optical absorption spectra of Ni²⁺-bearing compounds, S. Rossano, C. B., Phys. Chem. Min. (2000) 27 170



Fig. 1 A Optical absorption spectrum of a 0.25 mol l^{-1} solution of Ni(H₂O)²⁺₆ has been recorded in the UV-visible range on a CARY 5 spectrophotometer. Absorbance values have been transformed to absorption cross-section, σ (cm²) according to $\sigma = \ln(I_0/I)/dN_{at}$, where *d* is the cell size and N_{at} is the number of Ni atoms per m³. **B** Magnetic dipolar (*MD*) and electric quadrupolar (*EQ*) contribution to the theoretical absorption spectrum of Ni²⁺ ion in a regular octahedron. Parameter values are given in text

Peak positions are correctPeak intensities are wrong

Selection rules

3d-3d dipole transitions are forbidden

- In non-centrosymmetric sites, d and p states can mix by interacting with the ligands and dipole transitions are allowed
- In centrosymmetric sites, dipole transitions are still forbidden and transitions are allowed by vibrations
- Vibrations play a rôle in the width of the peaks
- Electron-phonon coupling



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Do you need to be a superhero?



Monica Rambeau alias Photon alias Spectrum alias Captain Marvel

The roads to progress

Energies

- TDDFT with improved kernel
- Multiplet approach with improved effective potential
- Many-body Green function techniques for quasi-degenerate systems

Intensities

- Taking vibrations into account
- Spectral shapes
 - Taking vibrations into account
 - Inelastic effects
- First-order effect

FOR YOUR ATTENTION



La mesure de l'absorption



Couleur du sang



Calcul de la couleur du sang

Nakatsuji et al. Chem. Phys. Lett. 256 (1996) 220
Orbitales symétrisées et configuration d'interaction
Symétrie Cs
48 atomes, 236 électrons
92350 états de symétrie A'
120182 états de symétrie A"



Couleur de l'herbe



Chlorophyll a





Calcul de la couleur de l'herbe

Hasegawa et al. J. Phys. Chem. 102 (1998) 1320
Orbitales symétrisées et configuration d'interaction
Symétrie C1
24971 états (fondamental)
71422 états (excité)



La couleur des minéraux

Couleur de la fayalite Fe₂SiO₄





O.V. Krasovska et al., Am. Min. 82 (1997) 672

Cr^{3+} (3d³) configuration t_2g^3



(b) t-orbitals

Hamiltonien effectif

Regardez le tableau Ecoutez le monsieur

$Cr^{3+}(3d^{3})$ terme ⁴F



Calculs perturbatifs

- Kristine Pierloot (2006)
- CASPT2 (complete active space with second order perturbation theory)
- La fonction de l'espace actif + les excitations simples et doubles.
- ◆ FeX₆, avec X=H₂O et X=NH₃

 Pour une précision de 1000 cm⁻¹, il faut aller jusqu'aux orbitales h sur le fer et aux orbitales f sur le ligand -> énorme calcul

The above conclusions may sound discouraging

Excitation triplet-singulet

 Deux orbitales, deux spins, 4 états • 4 états $|\uparrow\uparrow\rangle$, $|\uparrow\downarrow\rangle$, $|\downarrow\uparrow\rangle$ et $|\downarrow\downarrow\rangle$ Déterminants de Slater $\langle \uparrow \uparrow | H | \uparrow \uparrow \rangle = \langle \downarrow \downarrow | H | \downarrow \downarrow \rangle = J-K$ $\langle \uparrow \downarrow | H | \uparrow \downarrow \rangle = \langle \downarrow \uparrow | H | \downarrow \uparrow \rangle = J$ • Energie du triplet: $E_T = J - K$ • Energie du singlet: $E_s = J + K$ • $E_{s}=2\langle \uparrow \downarrow | H | \uparrow \downarrow \rangle - \langle \uparrow \uparrow | H | \uparrow \uparrow \rangle$

Fitter les multiplets: méthode

 Ziegler et al. Theor. Chim. Acta (1977) Daul (1993 - 2004), Moreno (1999-2008) • Exemple e^2 . Les orbitales e sont α et β . $E(^{1}A_{1}) = A + 8B + 4C + 2\varepsilon_{e} = 4E(\alpha^{+}\alpha^{-})/3 - E(\alpha^{+}\beta^{+})/3$ $E(^{3}A_{2})=A-8B+2\varepsilon_{e}=E(\alpha^{+}\beta^{+})$ $E(^{1}E) = A + 2C + 2\varepsilon_{e} = 2E(\alpha^{+}\alpha^{-})/3 + E(\alpha^{+}\beta^{+})/3$ Calcul SCF sur une molécule avec occupation 1/10 de chaque obitale d Calcul des énergies DFT des énergies des configurations • Fit des paramètres A, B, C, ε_e et ε_{t_2}

Fitter les multiplets: résultats

Garcia-Lastra et al. Phys. Rev. B 78, 085117 (2008)
Accord pour 10Dq

Emeraude : 15739 cm⁻¹ (théo) - 16130 cm⁻¹ (exp)
Spinelle : 20627 cm⁻¹ (théo) - 18520 cm⁻¹ (exp)
Rubis : 18179 cm⁻¹ (théo) - 18070 cm⁻¹ (exp)

Il est important d' avoir la bonne structure locale
Le champ de Madelung doit être pris en compte
Pas de calcul de l' intensité des transitions

Effet néphélauxétique

La répulsion coulombienne n' est pas la même dans les orbitales e et t₂.
Vision DFT: Fazzio, Caldas, Zunger (1984)
Watanabe, Kamimura (1987)
Ogasawara et al. (1998-2004)

Conclusion

Premier calcul ab initio convaincant

- Mais fondement théorique fragile
 - double-counting de la corrélation
 - prise en compte très approximative de l'influence des autres électrons
 - erreur sur l'intensité
 - réduction assez arbitraire des interaction electronelectron

Spectre nul pour un système centrosymétrique

Perspective

Traiter les systèmes centrosymétriques

- renir compte du couple électron-phonon
- commencer par un calcul en absorption X
- Améliorer le hamiltonien effectif
 - traiter le solide (et plus une molécule)
 - améliorer le calcul du potentiel dû aux autres électrons
 - améliorer le traitement de l'interaction électron-électron écrantée
 - Tenir compte des effets de champ local